

Fast Planning Through Planning Graph Analysis

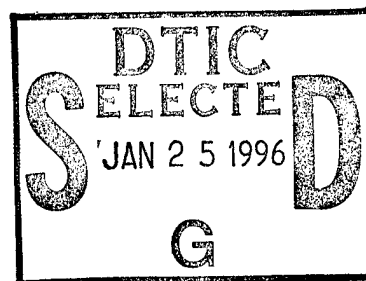
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Abstract

We introduce a new approach to planning in STRIPS-like domains based on constructing and analyzing a compact structure we call a Planning Graph. We describe a new planner, **Graphplan**, that uses this paradigm. **Graphplan** always returns a shortest-possible partial-order plan, or states that no valid plan exists.

We provide empirical evidence in favor of this approach, showing that **Graphplan** outperforms the total-order planner, Prodigy, and the partial-order planner, UCPOP, on a variety of interesting natural and artificial planning problems. We also give empirical evidence that the plans produced by **Graphplan** are quite sensible. Since searches made by this approach are fundamentally different from the searches of other common planning methods, they provide a new perspective on the planning problem.

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1 Introduction

In this paper we introduce a new planner, **Graphplan**, which plans in STRIPS-like domains. The algorithm is based on a paradigm we call Planning-Graph Analysis. In this approach, a compact structure called a *Planning Graph* is explicitly created that is then explored in a search. A Planning Graph is *not* a graph of “world-states” (which of course could be huge). Rather, Planning Graphs are closer in spirit to the PSGs of Etzioni [1990], and a plan is like a “flow” through this graph. Planning Graphs are structures based on domain information, the goals and initial conditions of a problem, and an explicit notion of time. Planning Graphs offer a convenient, efficient means of organizing and maintaining search information. They do so in a way that is reminiscent of the efficient solutions to Single-Source Shortest-Paths and Dynamic Programming problems. Planning Graph Analysis appears to have significant practical value in solving planning problems even though the inherent complexity of STRIPS-like planning, which is at least PSPACE-hard, is much greater than the complexity of Shortest-Paths or standard Dynamic Programming problems.

Graphplan combines aspects of both total-order and partial-order planners. Like traditional total-order planners, **Graphplan** makes strong commitments in its search. In fact, it makes even more commitments than most total-order planners because when it considers an action, it considers it at a specific point in time (not just a position in an ordering). For instance, it might consider placing the action ‘move Rocket1 from London to Paris’ in a plan at exactly time-step 2. It may seem puzzling that this kind of commitment could lead to fast planning, especially given the success enjoyed by least-commitment planners [Chapman, 1987][McAllester and Rosenblitt, 1991][Barrett and Weld, 1994][Weld, 1994]. However, the extra level of commitment allows **Graphplan** to store and manipulate valuable search information. This enables it to rapidly determine when backtracking is needed.

On the other hand, like partial-order planners, **Graphplan** generates partially ordered plans. For instance, in the rocket problem (Figure 1), the plan that **Graphplan** finds is of the form: “In time-step 1, appropriately load all the objects into the rockets, in time-step 2 move the rockets, and in time-step 3, unload the rockets.” The semantics of such a plan is that the actions in a given time step may be performed in any desired order. Conceptually this is a kind of “parallel” plan [Knoblock, 1994], since one could imagine executing the actions in three time steps if one had as many workers as needed to load and unload and fly the rockets.

One valuable feature of our algorithm is that it guarantees it will find the *shortest* plan among those in which independent actions may take place at the same time. Empirically and subjectively these sorts of plans seem particularly sensible. For example, in Stuart Russell’s “flat-tire world” (the goal is to fix a flat tire and then return all the tools back to where they came from; see the UCPOP domains list), the plan produced by **Graphplan** opens the boot (trunk) in step 1, fetches all the tools and the spare tire in step 2, inflates the spare and loosens the nuts in step 3, and so forth until it finally closes the boot in step 12. (See Figure 4.)

Another significant feature of our algorithm is that it is not particularly sensitive to the order of the goals in a planning task, unlike traditional approaches. More discussion of this issue is given in Section 3.2.

In Section 4 of this paper we present empirical results that demonstrate the effectiveness of **Graphplan** on a variety of interesting “natural” and artificial domains.

The rocket domain has three operators: Load, Unload, and Move. A piece of cargo can be loaded into a rocket if the rocket and cargo are in the same location. A rocket may move if it has fuel, but performing the move operation uses up the fuel. In UCPOP format, the operators are:

```
(define (operator move)
  :parameters ((rocket ?r) (place ?from) (place ?to))
  :precondition (:and (:neq ?from ?to) (at ?r ?from) (has-fuel ?r))
  :effect (:and (at ?r ?to) (:not (at ?r ?from)) (:not (has-fuel ?r))))

(define (operator unload)
  :parameters ((rocket ?r) (place ?p) (cargo ?c))
  :precondition (:and (at ?r ?p) (in ?c ?r))
  :effect (:and (:not (in ?c ?r)) (at ?c ?p)))

(define (operator load)
  :parameters ((rocket ?r) (place ?p) (cargo ?c))
  :precondition (:and (at ?r ?p) (at ?c ?p))
  :effect (:and (:not (at ?c ?p)) (in ?c ?r)))
```

A typical problem might have one or more rockets and some cargo in a start location with a goal of moving the cargo to some number of destinations.

Figure 1: A Simple Rocket Domain.

1.1 Definitions and Notation

Planning Graph Analysis applies to STRIPS-like planning domains [Fikes and Nilsson, 1971]. In these domains, operators have preconditions, add-effects, and delete-effects, all of which are conjuncts of propositions, and have parameters that can be instantiated to objects in the world. Operators do not create or destroy objects and time may be represented discretely. An example is given in Figure 1.

Specifically, by a *planning problem*, we mean:

- A STRIPS-like domain (a set of operators),
- A set of objects,
- A set of propositions (literals) called the Initial Conditions,
- A set of Problem Goals which are propositions that are required to be true at the end of a plan.

By an *action*, we mean a fully-instantiated operator. For instance, the operator ‘put ?x into ?y’ may instantiate to the specific action ‘put Object1 into Container2’. An

action taken at time t adds to the world all the propositions which are among its Add-Effects and deletes all the propositions which are among its Delete-Effects. It will be convenient to think of “doing nothing” to a proposition in a time step as a special kind of action we call a *no-op* or *frame* action.

2 Valid Plans and Planning Graphs

We now define what we mean when we say a set of actions forms a valid plan. In our framework, a *valid plan* for a planning problem consists of a set of actions and specified times in which each is to be carried out. There will be actions at time 1, actions at time 2, and so forth. Several actions may be specified to occur at the same time step so long as they do not interfere with each other. Specifically, we say that two actions *interfere* if one deletes a precondition or an add-effect of the other.¹ In a linear plan these *independent* parallel actions could be arranged in any order with exactly the same outcome. A valid plan may perform an action at time 1 if its preconditions are all in the Initial Conditions. It may perform an action at time $t > 1$ if the plan makes all its preconditions true at time t . Because we have no-op actions that carry truth forward in time, we may define a proposition to be true at time $t > 1$ if and only if it is an Add-Effect of some action taken at time $t - 1$. Finally, a valid plan must make all the Problem Goals true at the final time step.

2.1 Planning Graphs

A Planning Graph is similar to a valid plan, but without the requirement that the actions at a given time step not interfere. It is, in essence, a type of constraint graph that encodes the planning problem.

More precisely, a Planning Graph is a directed, leveled graph² with two kinds of nodes and three kinds of edges. The levels alternate between *proposition levels* containing *proposition nodes* (each labeled with some proposition) and *action levels* containing *action nodes* (each labeled with some action). The first level of a Planning Graph is a proposition level and consists of one node for each proposition in the Initial Conditions. The levels in a Planning Graph, from earliest to latest are: propositions true at time 1, possible actions at time 1, propositions possibly true at time 2, possible actions at time 2, propositions possibly true at time 3, etc.

Edges in a Planning Graph explicitly represent relations between actions and propositions. The action nodes in action-level i are connected by “precondition-edges” to their preconditions in proposition level i , by “add-edges” to their Add-Effects in proposition-level $i + 1$, and by “delete-edges” to their Delete-Effects in proposition-level $i + 1$.³

¹Knoblock [1994] describes an interesting less restrictive notion in which several actions may occur at the same time even if one deletes an add-effect of another, so long as those add-effects are not important for reaching the goals.

²A graph is called *leveled* if its nodes can be partitioned into disjoint sets L_1, L_2, \dots, L_n such that the edges only connect nodes in adjacent levels.

³A length-two path from an action a at one level, through a proposition Q at the next level, to an action b at the following level, is similar to a causal link $a \xrightarrow{Q} b$ in a partial-order planner.

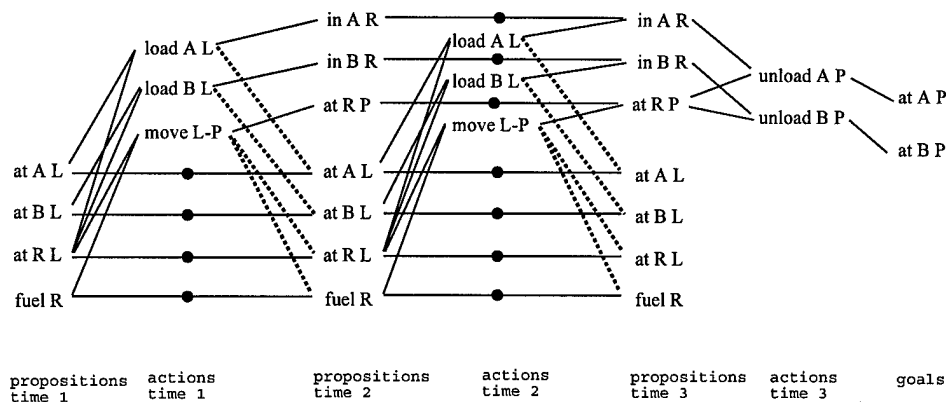


Figure 2: A planning graph for the rocket problem with one rocket *R*, two pieces of cargo *A* and *B*, a start location *L* and one destination *P*. For simplicity, the “rocket” parameter has been removed from the actions’ names. Delete edges are represented by dashed lines and no-ops are represented by dots. In the planning graph created by Graphplan for this problem, there would be more action nodes in the second and third action levels.

The conditions imposed on a Planning Graph are much weaker than those imposed on valid plans. Actions may exist at action-level i if all their preconditions exist at proposition-level i but there is no requirement of “independence.” In particular, action-level i may legally contain *all* the possible actions whose preconditions all exist in proposition-level i . A proposition may exist at proposition-level $i + 1$ if it is an Add-Effect of some action in action-level i (even if it is also a Delete-Effect of some other action in action-level i). Because we allow “no-op actions,” every proposition that appears in proposition-level i may also appear in proposition-level $i + 1$. An example of a Planning Graph is given in Figure 2.

Since the requirements on Planning Graphs are so weak, it is easy to create them. In Section 3.1 we describe how Graphplan constructs Planning Graphs from domains and problems. In particular, any Planning Graph with t action-levels that Graphplan creates will have the following property:

If a valid plan exists using t or fewer time steps, then that plan exists as a subgraph of the Planning Graph.

It is worth noting here that Planning Graphs are not overly large. See Theorem 1.

2.2 Exclusion Relations Among Planning Graph Nodes

An integral part of Planning-Graph Analysis is noticing and propagating certain *mutual exclusion* relations among nodes. Two actions at a given action level in a Planning Graph are *mutually exclusive* if no valid plan could possibly contain both. Similarly, two propositions at a given proposition level are mutually exclusive if no valid plan could possibly make both true. Identifying mutual exclusion relationships can be of enormous help in reducing the search for a subgraph of a Planning Graph that might correspond to a valid plan.

Graphplan notices and records mutual exclusion relationships by propagating them through the Planning Graph using a few simple rules. These rules do not guarantee to find *all* mu-

tual exclusion relationships, but usually find a large number of them.⁴ Specifically, there are two ways in which actions a and b at a given action-level are marked by Graphplan to be exclusive of each other:

[Interference] If either of the actions deletes a precondition or Add-Effect of the other. (This is just the standard notion of “non independence” and depends only on the operator definitions.)

[Competing Needs] If there is a precondition of action a and a precondition of action b that are marked as mutually exclusive of each other in the previous proposition level.

Two propositions p and q in a proposition-level are marked as exclusive if all ways of creating proposition p are exclusive of all ways of creating proposition q . Specifically, they are marked as exclusive if each action a having an add-edge to proposition p is marked as exclusive of each action b having an add-edge to proposition q .

For instance, in the rocket domain with ‘Rocket1 at London’ in the Initial Conditions, the actions ‘move Rocket1 from London to Paris’ and ‘load Alex into Rocket1 in London’ at time 1 are exclusive because the first deletes the proposition ‘Rocket1 at London’ which is a precondition of the second. The proposition ‘Rocket1 at London’ and the proposition ‘Rocket1 at Paris’ are exclusive at time 2 because all ways of generating the first (there is only one: a no-op) are exclusive of all ways of generating the second (there is only one: by moving). The actions ‘load Alex into Rocket1 in London’ and ‘load Jason into Rocket1 in Paris’ (assuming we defined the initial conditions to have Jason in Paris) at time 2 are exclusive because they have competing needs, namely the propositions ‘Rocket1 at London’ and ‘Rocket1 at Paris’.

A pair of propositions may be exclusive of each other at every level in a planning graph or they may start out being exclusive of each other in early levels and then become non-exclusive at later levels. For instance, if we begin with Alex and Rocket1 at London (and they are nowhere else at time 1), then ‘Alex in Rocket1’ and ‘Rocket1 at Paris’ are exclusive at time 2, but not at time 3.

2.2.1 The power of exclusion relations

Note that the Competing Needs notion and the exclusivity between propositions are not just logical properties of the operators. Rather, they depend on the interplay between operators and the Initial Conditions.

Consider, for instance, a domain such as the Rocket domain having a move operator. The useful notion that an item cannot be in two places at the same time is not just a function of the operators; if the initial conditions specified that the item started out in two different places, then it *could* continue to be in two places at once. Instead this notion depends both on the definition of ‘move’ and the fact that the item starts out in only one place. The mutual exclusion rules provide a mechanism for propagating this notion through the graph. The reason is that if at time $t - 1$ you can be in only one place, then any two move actions you might perform at time $t - 1$ will be exclusive (any two moves from *different*

⁴In fact, determining *all* mutual exclusion relationships can be as hard as finding a legal plan. For instance, consider creating two new artificial goals g_1 and g_2 such that satisfying g_1 requires satisfying half of the original goals and satisfying g_2 requires satisfying the other half.

starting locations are exclusive by **Competing Needs** and two moves from the *same* starting location are exclusive since they delete each others' preconditions) and therefore you can be in only one place at time t . Propagating these constraints allows the system to use this important fact in planning.

More generally, in many different domains, exclusion relations seem to propagate a variety of intuitively useful facts about the problem throughout the graph.

3 Description of the algorithm

The high-level description of our basic algorithm is the following. Starting with a Planning Graph that only has a single proposition level containing the Initial Conditions, **Graphplan** runs in stages. In stage i **Graphplan** takes the Planning Graph from stage $i - 1$, extends it one time step (the next action level and the following proposition level), and then searches the extended Planning Graph for a valid plan of length i . **Graphplan**'s search either finds a valid plan (in which case it halts) or else determines that the goals are not all achievable by time i (in which case it goes on to the next stage). Thus, in each iteration through this Extend/Search loop, the algorithm either discovers a plan or else proves that no plan having that many time steps or fewer is possible.

Graphplan's algorithm is sound and complete: any plan the algorithm finds is a legal plan, and if there exists a legal plan then **Graphplan** will find one. In Section 5 we describe how this algorithm may be augmented so that if the Problem Goals are not satisfiable by *any* valid plan, then the planner is guaranteed to halt with failure in finite time. This termination guarantee is one that is not provided by most partial-order planners.

3.1 Extending Planning Graphs

All the initial conditions are placed in the first proposition level of the graph. To create a generic action level, we do the following. For each operator and each way of instantiating preconditions of that operator to propositions in the previous level, insert an action node *if no two of its preconditions are labeled as mutually exclusive*.⁵ Also insert all the no-op actions and insert the precondition edges. Then check the action nodes for exclusivity as described in Section 2.2 above and create an "actions-that-I-am-exclusive-of" list for each action.

To create a generic proposition level, simply look at all the Add-Effects of the actions in the previous level (including no-ops) and place them in the next level as propositions, connecting them via the appropriate add and delete-edges. Mark two propositions as exclusive if all ways of generating the first are exclusive of all ways of generating the second.

As we demonstrate in the following theorem, the time taken by our algorithm to create this graph structure is polynomial in the length of the problem's description and the number of time steps.

Theorem 1 *Consider a planning problem with n objects, p propositions in the Initial Conditions, and m STRIPS operators each having a constant number of formal parameters. Let*

⁵Checking for exclusions keeps **Graphplan**, for instance, from inserting the action 'unload Alex from Rocket1 in Paris' in time 2 of the rocket-domain graph when the initial conditions specify that both Alex and the rocket begin in London.

ℓ be the length of the longest add-list of any of the operators. Then, the size of a t -level planning graph created by Graphplan, and the time needed to create the graph, are polynomial in n , m , p , ℓ , and t .

Proof. Let k be the largest number of formal parameters in any operator. Since operators cannot create new objects, the number of different propositions that can be created by instantiating an operator is $O(\ell n^k)$. So, the maximum number of nodes in any proposition-level of the planning graph is $O(p + m\ell n^k)$. Since any operator can be instantiated in at most $O(n^k)$ distinct ways, the maximum number of nodes in any action-level of the planning graph is $O(mn^k)$. Thus the total size of the planning graph is polynomial in n , m , p , ℓ , and t , since k is constant.

The time needed to create a new action and proposition level of the graph can be broken down into (A) the time to instantiate the operators in all possible ways to preconditions in the previous proposition-level, (B) the time to determine mutual exclusion relations between actions, and (C) the time to determine the mutual exclusion relations in the next level of propositions. It is clear that this time is polynomial in the number of nodes in the current level of the graph. ■

Empirically, the part of graph creation that takes the most time is determining exclusion relations. However, empirically, graph creation only takes up a significant portion of Graphplan's running time in the simpler problems, where the total running time is not very large anyway.

An obvious improvement to the basic algorithm described above (which is implemented in Graphplan) is to avoid searching until a proposition-level has been created in which all the Problem Goals appear and no pair of Problem Goals has been determined to be mutually exclusive.

3.2 Searching for a plan

Given a Planning Graph, Graphplan searches for a valid plan using a backward-chaining strategy. Unlike most other planners, however, it uses a level-by-level approach, in order to best make use of the mutual exclusion constraints. In particular, given a set of goals at time t , it attempts to find a set of actions (no-ops included) at time $t - 1$ having these goals as add effects. The preconditions to these actions form a set of subgoals at time $t - 1$ having the property that if *these* goals can be achieved in $t - 1$ steps, then the original goals can be achieved in t steps. If the goal set at time $t - 1$ turns out not to be solvable, Graphplan tries to find a different set of actions, continuing until it either succeeds or has proven that the original set of goals is not solvable at time t .

In order to implement this strategy, Graphplan uses the following recursive search method. For each goal at time t in some arbitrary order, select some action at time $t - 1$ achieving that goal that is not exclusive of any actions that have already been selected. Continue recursively with the next goal at time t . (Of course, if by good fortune a goal has already been achieved by some previously-selected action, we do not need to select a new action for it.) If our recursive call returns failure, then try a different action achieving our current goal, and so forth, returning failure once all such actions have been tried. Once finished with all the goals at time t , the preconditions to the selected actions make up the new goal

set at time $t - 1$. We call this a "goal-set creation step." Graphplan then continues this procedure at time step $t - 1$.

A "forward-checking" improvement to this approach (which is implemented in Graphplan and helps modestly in our experiments) is that after each action is considered a check is made to make sure that no goal ahead in the list has been "cut-off." In other words, Graphplan checks to see if for some goal still ahead in the list, all the actions creating it are exclusive of actions we have currently selected. If there is some such goal, then Graphplan knows it needs to back up right away.

3.2.1 Memoization

One additional aspect of Graphplan's search is that when a set of (sub)goals at some time i is determined to be not solvable, then before popping back in the recursion it *memoizes* what it has learned, storing the goal set and the time i in a hash table. Similarly, when it creates a set of subgoals at some time i , before searching it first probes the hash table to see if the set has already been proved unsolvable. If so, it then backs up right away without searching further. This memoizing step, in addition to its use in speeding up search, is needed for our termination check described in Section 5.

3.2.2 An example

To make this more concrete, let us consider again the rocket problem in which the Initial Conditions have two fueled rockets and n pieces of cargo at some starting location S and the goal is to move some of the cargo to location X and some to location Y . For this problem, the graph will grow to contain three action levels. The planner will then select some goal, say 'A at X', and pick some action at time step 3 such as 'unload A from Rocket1 at X' making it true. It then marks as not-doable all actions exclusive of this one, such as 'unload C from Rocket1 at Y', at time step 3. The planner then selects the next goal, say 'B at X'. If it chooses to make this goal true by performing 'unload B from Rocket2 at X' at time 3, then it will notice that a goal such as 'C at Y' further down in its goal list has been completely cut off, because all ways of making it true are exclusive of the actions already committed to. Thus, Graphplan will instead select 'unload B from Rocket1 at X', and so on. Once the planner is done with all goals at this level, it then creates a new goal-set at the previous time step consisting of goals such as 'A in Rocket1' and 'Rocket1 at X' that were the preconditions of the actions selected.

3.2.3 The limited effect of goal orderings

The strategy of working on the subgoals in a somewhat breadth-first-like manner makes Graphplan fairly insensitive to goal-orderings. We now add one final feature to Graphplan's search strategy that will allow us to make this statement more precise. Let G be a goal set at some time t . We say that a non-exclusive set of actions A at time $t - 1$ is a *minimal set of actions achieving G* if (1) every goal in G is an add-effect of some action in A , and (2) no action can be removed from A so that the add effects of the actions remaining still contain G . The modification to Graphplan's strategy is to only recurse on minimal action sets. If the set of actions A chosen by Graphplan to achieve some goal-set G is *not* minimal, we back up right away. (For instance, say our goals are g_1 and g_2 ; we pick some action

achieving g_1 but then the action we choose to achieve g_2 happens to also achieve g_1 as well. This would not be minimal.) This modification allows us to make a clean statement about the goal-sets that **Graphplan** considers. Specifically, we can state the following theorem.

Theorem 2 *Let G be a goal set at some time t that is not solvable in t steps. Then, no matter what the ordering of the goals in G , the goal sets at time $t - 1$ that **Graphplan** considers when attempting to achieve G are exactly the preconditions of all the minimal action sets at time $t - 1$ achieving G . (If G is solvable in t steps, then **Graphplan** may halt before considering all those goal sets).*

Proof. We have forced **Graphplan** to consider *only* minimal action sets; we need to show that *every* such set is examined. Let A be some such set, and consider some arbitrary ordering of G . Let a_1 be some action in A achieving the first goal in G (and let's call that goal g_{a_1}). Let a_2 be the action in A achieving the first goal in G not already achieved by a_1 (and let's call that goal g_{a_2}). More generally, let a_i be the action in A achieving the first goal in G not achieved by any of $\{a_1, \dots, a_{i-1}\}$, and we will call that goal g_{a_i} . Notice that all actions in A are given an index in this way because A is minimal. This ordering of the actions implies that at some point in the recursion, a_1 will be the action chosen by **Graphplan** to achieve goal g_{a_1} ; given that that occurs, at some point a_2 will be the action chosen to achieve g_{a_2} , and so forth. Therefore, all actions in A are considered. ■

We can now quantify the limited effect of goal ordering as follows. Suppose **Graphplan** is currently attempting to solve the Problem Goals at some time T and is unsuccessful. Then, the total number of goal-sets examined in the search is *completely independent of* the ordering of the goals. The effect of goal ordering is limited to (A) the amount of time it takes on average to examine a new goal set (perform a goal-set creation step), and (B) the amount of work performed in the final stage at which the Problem Goals *are* found to be solvable (since goal ordering may affect the order in which goal sets are examined). In addition to this theoretical statement, empirically, **Graphplan**'s dependence on goal ordering seems to be quite small: significantly less than that of other planners such as Prodigy and UCPOP.

4 Experimental Results

4.1 Natural domains

We compared **Graphplan** with two popular planners, Prodigy and UCPOP, on several "natural" planning problems. We ran Prodigy with heuristics suggested in Stone et al. [Stone et al., 1994] and by Carbonell [Carbonell, personal communication]. Note that **Graphplan** is written in C while the other planners are in compiled Lisp. On the other hand, we ran **Graphplan** on a (slow) DECstation 2100 and the other planners on a (faster) SPARC10.

In addition to running time, we also report for **Graphplan** the number of goal-set creation steps (the number of times it creates a goal set at time $t - 1$ from a goal set at time t) and the total number of times that it selects a non-noop action to try. These are somewhat analogous to the backward-chaining steps taken by total-order planners.

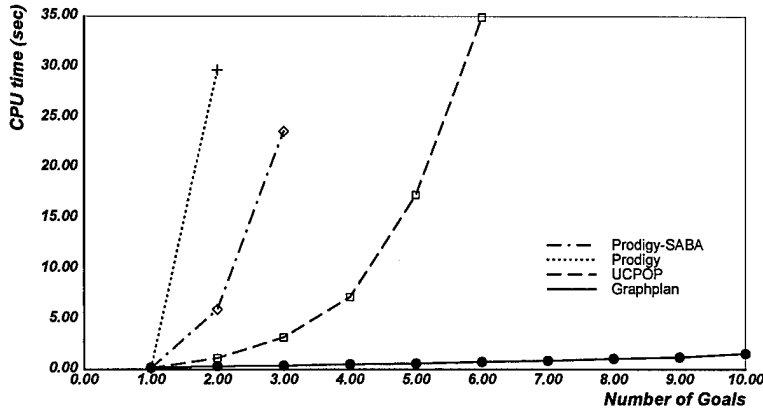


Figure 3: 2-Rockets problem

4.1.1 Rocket

We ran the planners on the rocket domain described in Figure 1 with the following setup. The initial conditions have 3 locations (London, Paris, JFK), two rockets, and n items of cargo. All the objects (rockets and cargo) begin at London and the rockets have fuel. The goal is to get $\lceil n/2 \rceil$ of the objects to Paris and $\lfloor n/2 \rfloor$ of the objects to JFK. The goals are ordered alternating between destinations.

Results of the experiment are in Figure 3. Notice that **Graphplan** significantly outperforms the other two planners on this domain. **Graphplan** does well in this domain for two main reasons: (1) the Planning Graph only grows to 3 time steps, and (2) the mutual exclusion relations allow a small number of commitments (unloading something from Rocket1 in Paris and something else from Rocket2 in JFK) to completely force the remainder of the decisions. In particular, **Graphplan** performs only two goal-set creation steps regardless of the number of goals, and the number of non-noop actions tried is linear in the number of goals. The size of the graph created is also linear in the number of goals: there are 150 nodes total for the problem with two goals, and 37 additional nodes per goal from then on.

The running time of **Graphplan** is completely unaffected by goal ordering for this problem.

4.1.2 Flat Tire

A natural problem of a different sort is Stuart Russell's "fixing a flat tire" scenario (domain `init-flat-tire`, problem `fixit` in the UCPOP distribution). Unlike the rocket domain, a valid plan for solving this problem requires at least 12 time steps (and 19 actions). While for the rocket domain, **Graphplan** would do pretty well even without the mutual exclusion propagation, here the mutual exclusions are critical and ensure that not too many goal sets will be examined. **Graphplan** solves this problem in 1.1 to 1.3 seconds depending on the goal ordering. The number of goal-set creation steps ranges from a minimum of 105 to a maximum of 246, and the number of non-noop actions tried from 170 to 350. The final graph created contains 786 nodes. Neither UCPOP nor Prodigy found a solution within 10 minutes for this problem in the standard goal ordering, though it is possible to find goal orderings where they succeed much more quickly. **Graphplan** is not only fast on this domain, but also by producing the shortest partial-order plan, its plan is intuitively

Step 1:	open boot
Step 2:	fetch wrench boot fetch pump boot fetch jack boot fetch wheel2 boot
Step 3:	inflate wheel2 loosen nuts the-hub
Step 4:	put-away pump boot jack-up the-hub
Step 5:	undo nuts the-hub
Step 6:	remove-wheel wheel1 the-hub
Step 7:	put-on-wheel wheel2 the-hub put-away wheel1 boot
Step 8:	do-up nuts the-hub
Step 9:	jack-down the-hub
Step 10:	put-away jack boot tighten nuts the-hub
Step 11:	put-away wrench boot
Step 12:	close boot

Figure 4: Graphplan's plan for Russell's "Fixit" problem.

"sensible". Figure 4 shows the plan produced by Graphplan for this problem.

4.1.3 Monkey and Bananas

The UCPOP distribution provides three "Monkey and Bananas" problems (originally from Prodigy). Two have a solution and the third does not. Srinivasan and Howe [Srinivasan and Howe, 1995] show experimental results for a variety of partial-order planning heuristics on this domain. They report average running times (on a SPARC IPX, in Common Lisp) of about 90 seconds for most of the methods, though one took 2000 seconds and one took only 30 seconds on average per problem. They report an average number of plans examined in those planners for a task called "flaw selection" ranging from 5,558 to 105,518. Graphplan solves these problems much more quickly, taking 0.7 seconds on the first, 3.4 seconds on the second, and 2.8 seconds on the unsolvable one (these times are on a DECstation 2100). Graphplan attempts only 6 non-noop actions in solving the first problem, and 90 on the second. On the unsolvable problem, Graphplan extends its graph to 7 time steps, at which point it notices that the problem is unsolvable because the graph has "leveled off" and yet there still remain exclusive goals (see Section 5).

On all three problems, most of the time spent is in graph creation. The graphs for the three problems contain 304, 824, and 700 nodes, respectively.

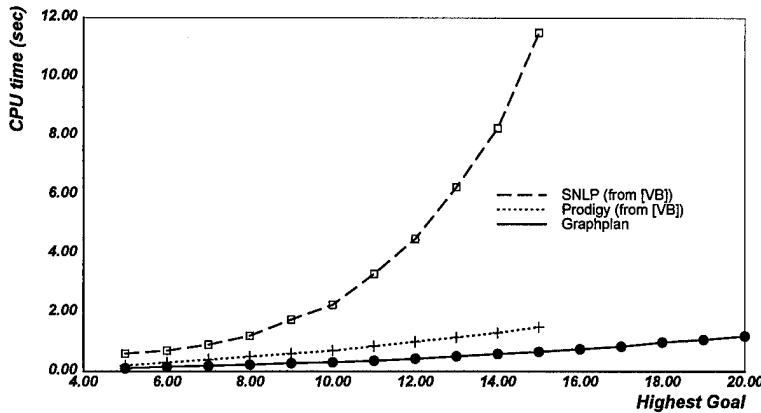


Figure 5: *Link-repeat domain from (Veloso & Blythe 1994)*

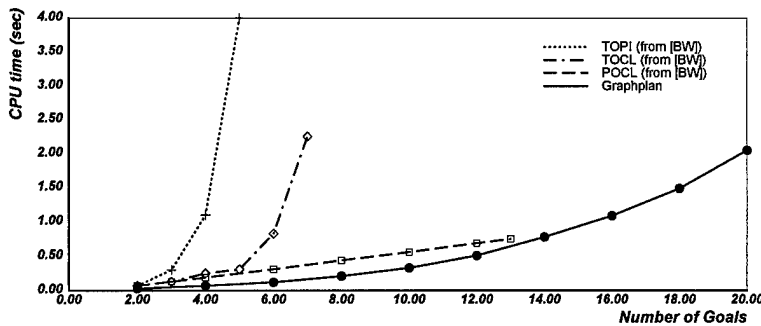


Figure 6: $D^1 S^1$ domain from (Barrett & Weld 1994)

4.1.4 The Fridge Domain

The UCPOP distribution provides two “refrigerator fixing” domains. On the first one, *Graphplan* takes 4.0 seconds, performs 2 goal-set creation steps, and attempts 7 non-noop actions. On the second one *Graphplan* takes 11.3 seconds, performs 46 goal-set creation steps, and attempts 258 actions. On these two problems, the graphs created contain 287 and 686 nodes, respectively.

Srinivasan and Howe [1995] report times ranging from 30 to 300 seconds and average number of plans examined from about 9700 to 42000 for the different methods they consider.

4.2 Artificial domains

Barrett and Weld [1994] and Veloso and Blythe [1994] define a collection of artificial domains intended to distinguish the performance characteristics of various planners. On all of these, *Graphplan* is quite competitive with the best performance reported.

We present in Figures 5, 6, 7, and 8 performance data on four of the more interesting domains. All performance results in these figures for the other planners are taken from figures in their respective papers.

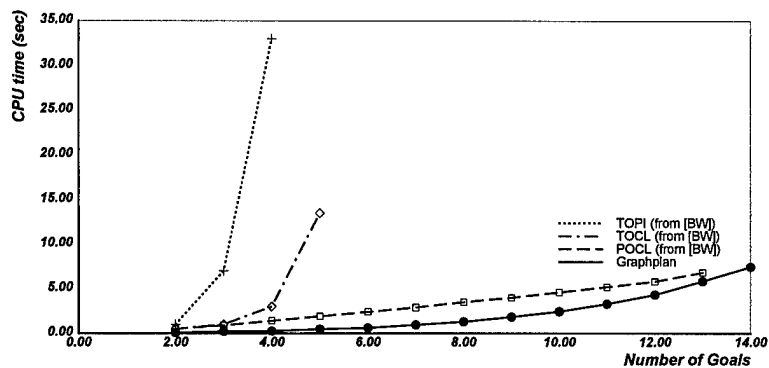


Figure 7: $D^1 S^2$ domain from (Barrett & Weld 1994)

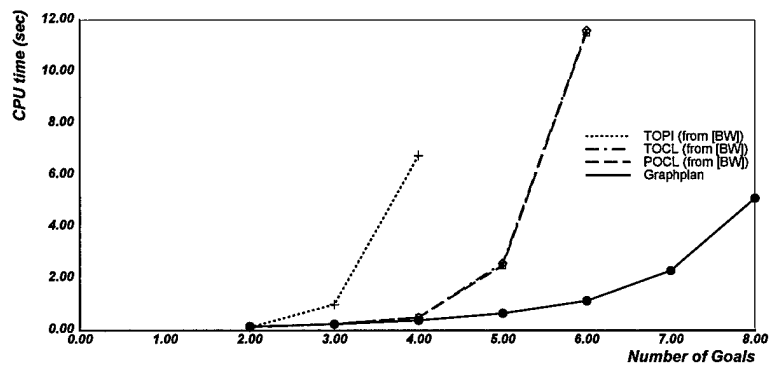


Figure 8: $D^m S^{2*}$ domain from (Barrett & Weld 1994)

4.3 Discussion of Experimental Results

Four major factors seem to account for most of Graphplan's efficiency. They are, in order of empirically-derived importance:

Mutual Exclusion: The propagation and extensive use of mutual exclusion relations effectively prunes a large part of the search space.

Consideration of Parallel Plans: In some cases, such as the rocket problem, the valid parallel plans are relatively short compared with the length of the corresponding totally-ordered plans. In such cases neither the cost of Planning Graph construction, nor the cost of search is very large.

Memoizing: By fixing actions at specific points in time, Graphplan is able to record the goal sets that it proves to be unreachable in a certain number of time steps from the initial conditions.

Low-level costs: By constructing a Planning Graph in advance of search, Graphplan avoids the costs of performing instantiations during the searching phase.

It is interesting to note that in three out of four of these points Graphplan's commitment to putting specific actions at specific points in time plays an important role.

5 Terminating on Unsolvable Problems

To a first approximation, Graphplan conducts something like an iteratively-deepened search. In the i^{th} stage the algorithm sees if there is a valid parallel plan of length less than or equal to i . As described so far, if no valid plan exists there is nothing that prevents the algorithm from mindlessly running forever through an infinite number of stages.

We now describe a simple and efficient test that can be added after every unsuccessful stage so that if the problem has no solution then Graphplan will eventually halt and say "No Plan Exists."

5.1 Planning Graphs "Level Off"

Assume a problem has no valid plan. First observe that in the sequence of Planning Graphs created there will eventually be a proposition level P such that all future proposition levels are exactly the same as P , *i.e.*, they contain the same set of propositions and have the same exclusivity relations.

The reason for this is as follows. Because of the no-op actions, if a proposition appears in some proposition level then it also appears in all future proposition levels. Since only a finite set of propositions can be created by STRIPS-style operators (when applied to a finite set of initial conditions) there must be some proposition level Q such that all future levels have exactly the same set of propositions as Q . Also, again because of the no-op actions, if propositions p and q appear together in some level and are *not* marked as mutually exclusive, then they will not be marked as mutually exclusive in any future level. Thus there must be some proposition level P after Q such that all future proposition levels also have exactly the same set of mutual exclusion relations as P .

In fact, it is not hard to see that once two adjacent levels P_n, P_{n+1} are identical, then all future levels will be identical to P_n as well. At this point, we say the graph has *leveled off*.

5.2 A Test to Guarantee Termination

Let P_n be the first proposition level at which the graph has leveled off. If some Problem Goal does not appear in this level, or if two Problem Goals are marked as mutually exclusive in this level, then **Graphplan** can immediately say that no plan exists. However, it may be the case that no plan exists but this simple test does not detect it, so we need to do something slightly more sophisticated to guarantee termination.

As mentioned earlier, **Graphplan** memoizes, or records, goal sets that it has considered at some level and determined to be unsolvable. Let S_i^t be the collection of all such sets stored for level i after an unsuccessful stage t . In other words, after an unsuccessful stage t , **Graphplan** has determined two things: (1) any plan of t or fewer steps must make one of the goal sets in S_i^t true at time i , and (2) none of the goal sets in S_i^t are achievable in i steps. The modification to **Graphplan** ensure termination is now just the following:

If the graph has leveled off at some level n and a stage t has passed in which $|S_n^{t-1}| = |S_n^t|$, then output "No Plan Exists."

Theorem 3 *Graphplan outputs "No Plan Exists" if and only if the problem is unsolvable.*

Proof. The easy direction is that if the problem is unsolvable, then **Graphplan** will eventually say that no plan exists. The reason is just that the number of sets in S_n^t is never *smaller* than the number of sets in S_n^{t-1} , and there is a finite maximum (though exponential in the number of nodes at level n).

To see the other direction, suppose the graph has leveled off at some level n and **Graphplan** has completed an unsuccessful stage $t > n$. Notice that any plan to achieve some set in S_{n+1}^t must, one step earlier, achieve some set in S_n^t . This is because of the way **Graphplan** works: it determined each set in S_{n+1}^t was unsolvable by mapping it to sets at time step n and determining that they were unsolvable. Notice also that since the graph has leveled off, $S_{n+1}^t = S_n^{t-1}$. That is because the last $t - n$ levels of the graph are the same no matter how many additional levels the graph has.

Now suppose that after an unsuccessful stage t , $|S_n^{t-1}| = |S_n^t|$ (which implies that $S_n^{t-1} = S_n^t$). This means that $S_{n+1}^t = S_n^t$. Thus, in order to achieve any set in S_{n+1}^t one must previously have achieved some other set in S_{n+1}^t . Since none of the sets in S_{n+1}^t are contained in the initial conditions, the problem is unsolvable. ■

6 Additional Features

We have discussed so far the basic algorithm used by **Graphplan**. We now describe a few additional features that can be added in a natural way (and have been added as options in our implementation), and discuss their significance.

The first feature is a type of reasoning that is quite natural in our framework. The reasoning is that if the current goal set contains n goals such that no two of them can be made true at the same time by a non-noop action (and none of them are present in the Initial Conditions), then any plan will require n steps. For instance, one could use this reasoning in a path-finding domain to show that it must take at least n steps to visit n distinct places. Unfortunately, finding the largest such subset of any given goal set is equivalent to the maximum Clique problem (think of there being a “can’t both be created now” edge between any two propositions that cannot both be made true in the same step). However, we can find a *maximal* such set using greedy methods.

This form of reasoning turns out to be very useful on traveling-salesman-like problems. On very dense graphs (such as the complete graph) for which the problem should be easy, **Graphplan** without this reasoning can be quite slow because the pairwise exclusion relations do not propagate well. For instance, on a complete graph, after two time steps any two goals of the form ‘visited X’ will be non-exclusive. However, with this reasoning, **Graphplan**’s performance is more respectable.

A second feature concerns graph creation. Although, as demonstrated in Theorem 1, the graph size is polynomial, it may be unnecessarily large if there are many irrelevant facts in the initial conditions. One way around this problem is to begin with a regression analysis going backward from the goals to determine if any initial conditions may be thrown out. For instance, if our rocket problem contains a “junkyard” of rockets with no fuel in the initial conditions, or some number of irrelevant observers, this method can identify them and set them aside. Of course, performing this regression analysis itself takes some amount of time.

One final feature (not currently in our implementation) that could be added easily is the ability to use the information learned on one planning problem for another problem on the same domain having the same Initial Conditions. Specifically, the same graph and the same memoized unsolvable goal sets could be re-used in this case.

7 Discussion and Future Work

We have described a novel planning algorithm, **Graphplan**. This algorithm uses ideas from standard total-order and partial-order planners, but differs most significantly by taking the position that representing the planning problem in a graph structure — a structure one can analyze, annotate, and play with — will greatly improve efficiency. Performance on the problems we have tried indicate that indeed this can provide a great savings.

We believe that even more significant gains will come from combining the approach of **Graphplan** with ideas, heuristics, and learning methods that have been developed in the planning literature. Specifically, directions we are currently considering include:

Learning: Learning techniques found to be useful for other planning methods (e.g., [Etzioni, 1990]) may work here as well. In addition, perhaps the new representation used here will suggest other learning approaches not considered previously.

Symmetry detection: Many of the times that planners behave poorly are times when symmetries exist in a problem that the planner does not utilize. Representing the

planning problem as a graph may allow for new methods of detecting symmetries that could drastically reduce the search needed.

Operator ordering: Currently if *Graphplan* is allowed to place additional time steps into the graph (and not produce a minimal plan) it does not use those extra time steps well. Operator-ordering heuristics may allow *Graphplan* to more quickly find a non-minimal plan, if that is desired. For reasons similar to that in Theorem 2, however, we do not expect operator ordering to help in more quickly proving that a problem is *not* solvable in a given number of time steps.

Two-way searches: Some problems are more easily solved in the forward direction than in the reverse. *Prodigy*, for instance, is able to create a plan in a forward direction even while it searches from the goals. We would like to incorporate some method for planning in a similar manner. This might involve memoizing solvable goal sets as well as unsolvable ones.

Other information to propagate: *Graphplan* propagates pairwise exclusion relations in order to speed up its search. There may be other sorts of information that could be propagated forward or backward through the graph that would be useful as well.

The original motivation for our approach was that planning graphs, with slight modification, allow one to think of planning as a certain kind of maximum flow problem.⁶ The view of planning as a flow problem requires additional constraints that make the problem NP-hard (in particular, a constraint that certain edges be either unused or else fully saturated, corresponding to the fact that an action may be performed or not performed, but cannot be “partially performed”). Nonetheless, perhaps algorithms for the max-flow problem — and there are many fast algorithms known [Cormen *et al.*, 1990, Goldberg and Tarjan, 1986] — might be useful for guiding the planning process. Empirically, we found that an approach based solely on max-flow algorithms did not perform as well as the method of backward-chaining with mutual exclusion relations described in this paper. A flow-based method, however, may allow one to naturally incorporate other aspects of a planning problem, such as having different costs associated with different actions, in a natural way. We are currently exploring whether flow algorithms can be *combined* with our current approach to improve performance.

Accessing Graphplan

Graphplan is available via <http://www.cs.cmu.edu/~avrim/graphplan.html>.

Acknowledgements

We thank Jaime Carbonell and the members of the CMU Prodigy group for their helpful advice.

⁶In this problem, one is given a graph containing source and sink nodes, and each edge is labeled with a capacity representing the maximum amount of fluid that may flow across that edge. In a legal flow, for every node except the source or sink, the flow in must equal the flow out. The goal is to flow as much fluid as possible from the source to the sink, without exceeding any of the capacities.

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NOTE OF EXPLANATION FOR SELECTION, JOA # 234-95SK (A)

1. I selected Mr. Barry L. Christensen for the Program Analysts, GS-343-12 position in DTIC-OCP.
2. In comparing the candidates against each of the selection criteria, Mr. Christensen's credentials were such that I'm firmly convinced he is the best qualified to perform the duties and responsibilities of the position. I've had discussion with his current and previous supervisors and they speak very highly of the selectee. His performance is consistently at the "5" performance level and he has received two "on-the-spot" awards recently for outstanding contributions to the DLA mission. I've reviewed samples of Mr. Christensen's writing and find it outstanding; his impromptu speaking skills seem outstanding as well. His honed oral and written communication skills played a big part in my selecting him for this position.
3. Mr. Christensen was the best educated of the available candidates. He has completed several management and computer courses and currently working on his masters degree. He has a strong math background which is indicative of someone who thinks analytically--and I need that quality in -OCP.

FRANK V. SCOTT, JR.
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